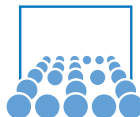


High Performance and Parallel Computing
for Materials Defects and Multiphase Flows

Dynamic Rupture Earthquake Simulations on Petascale Heterogeneous Supercomputers

M. Bader, A. Breuer, S. Rettenberger,
A.-A. Gabriel, C. Pelties, A. Heinecke

Singapore, 14 Jan 2015



SeisSol Core Developers



Alexander
Breuer



Alice-Agnes
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Christian
Pelties



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Overview and Agenda

Dynamic Rupture and Earthquake Simulation with SeisSol:

- unstructured tetrahedral meshes
- high-order ADER-DG discretisation
- target applications: earthquake dynamics, tsunami generation

Towards Scalable I/O:

- two-stage scheme to generate and read mesh partitions
- improve scalability of output and checkpointing

Optimisation for Heterogeneous Petascale Platforms:

- code generation to optimize element-local matrix kernels
- offload scheme to address multiphysics

Petascale Runs on Tianhe-2, Stampede and SuperMUC:

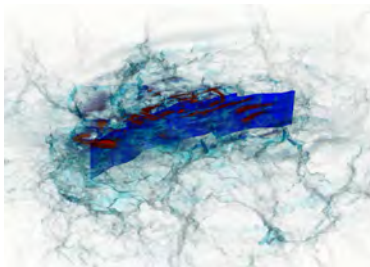
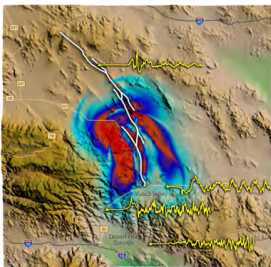
- weak scaling of wave propagation component
- strong scaling for 1992 Landers M7.2 earthquake

Part I

Dynamic Rupture and Earthquake Simulation with SeisSol

<http://seissol.geophysik.uni-muenchen.de/>

Dynamic Rupture and Earthquake Simulation

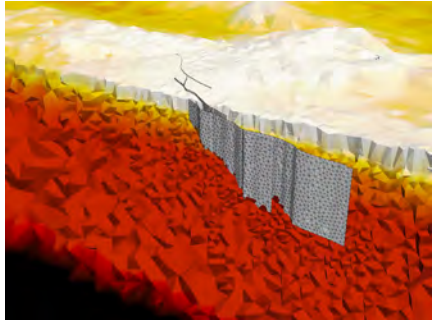
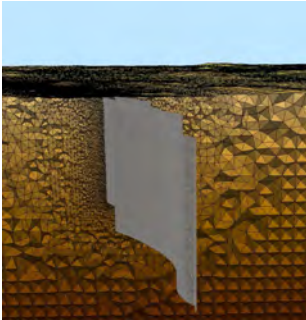


Landers fault system: simulated ground motion and seismic waves

SeisSol – ADER-DG for seismic simulations:

- adaptive tetrahedral meshes
→ complex geometries, heterogeneous media, multiphysics
- complicated fault systems with multiple branches
→ non-linear multiphysics dynamic rupture simulation
- ADER-DG: high-order discretization in space and time

1992 Landers M7.2 Earthquake



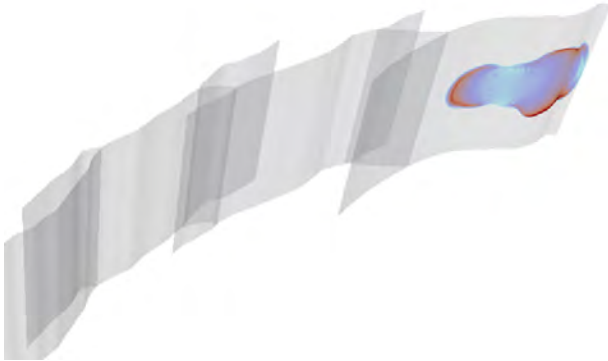
- multiphysics simulation of dynamic rupture and resulting ground motion of a M7.2 earthquake
- fault inferred from measured data, regional topography from satellite data, physically consistent stress and friction parameters
- 1D velocity structure, low velocity near surface

Multiphysics Dynamic Rupture Simulation



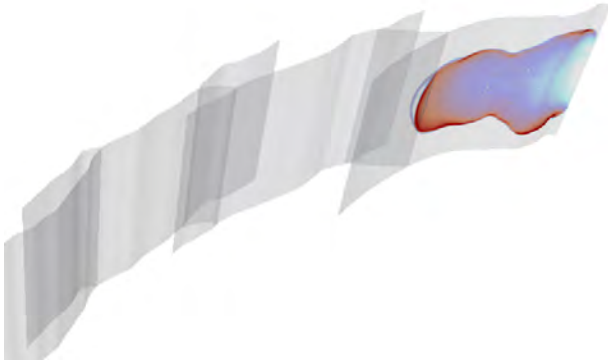
- spontaneous rupture, non-linear interaction with wave-field
- featuring rupture jumps, fault branching, etc.
- tackles fundamental questions on earthquake dynamics
- realistic rupture source for seismic hazard assessment

Multiphysics Dynamic Rupture Simulation



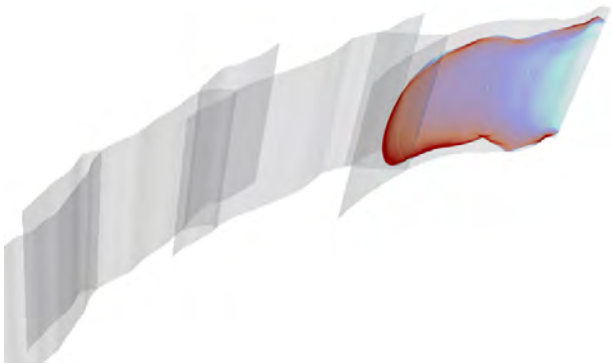
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Multiphysics Dynamic Rupture Simulation



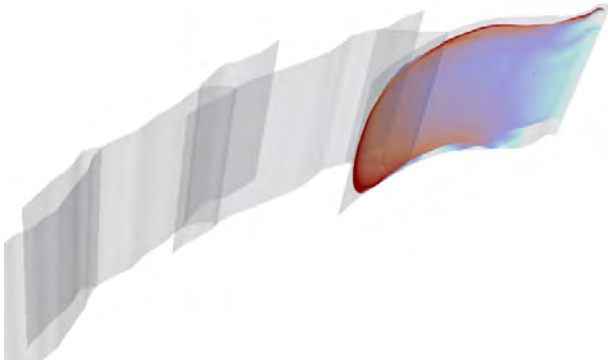
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Multiphysics Dynamic Rupture Simulation



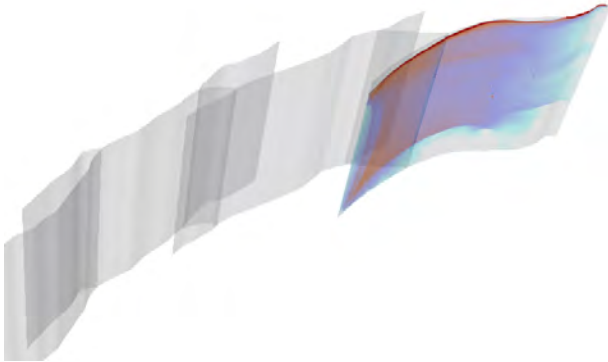
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Multiphysics Dynamic Rupture Simulation



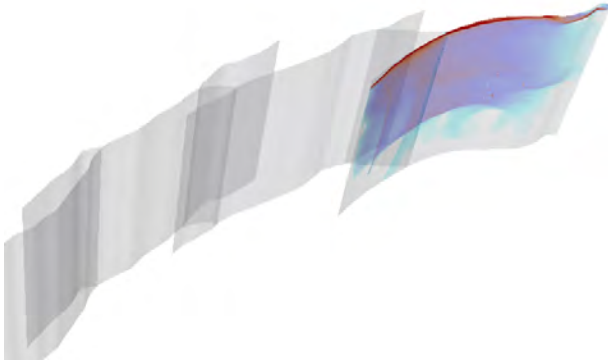
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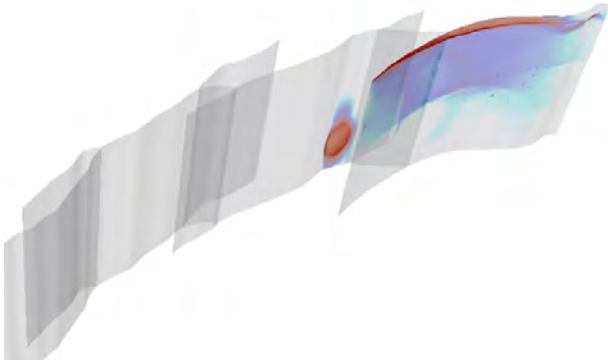
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Multiphysics Dynamic Rupture Simulation



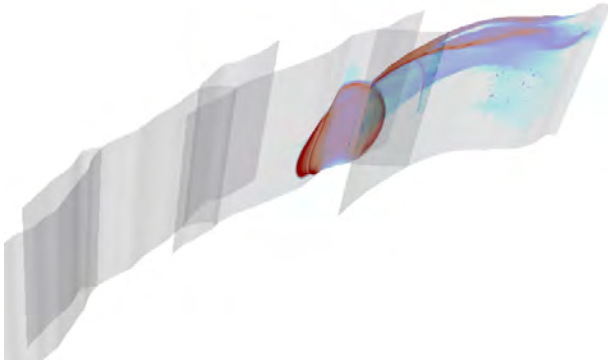
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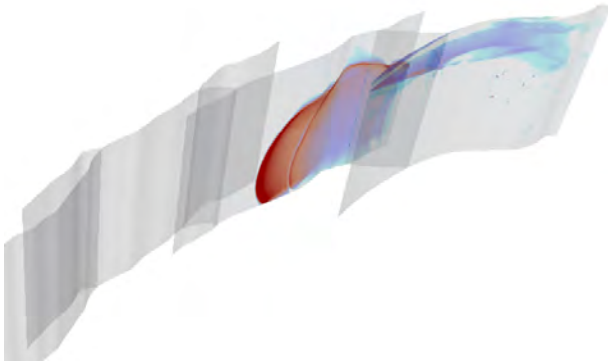
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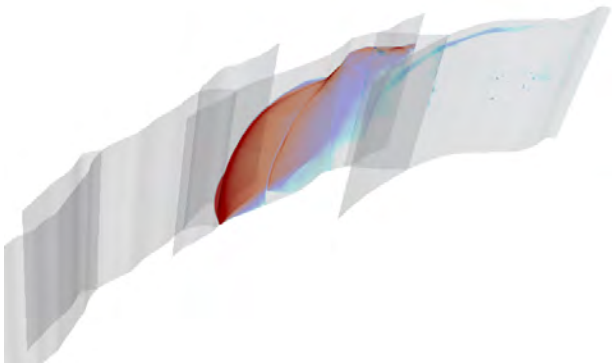
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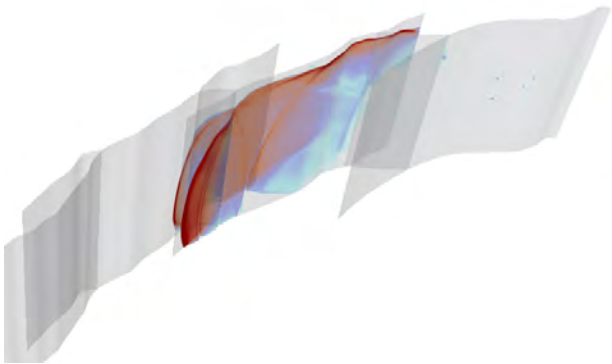
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Multiphysics Dynamic Rupture Simulation



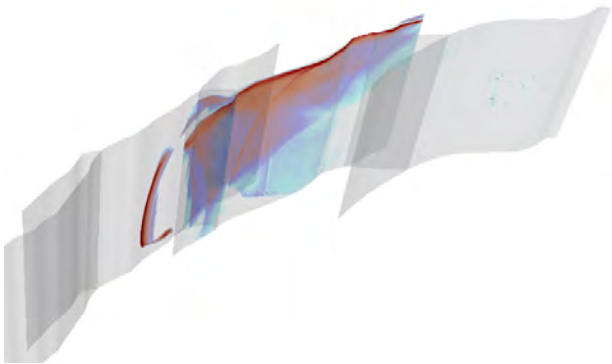
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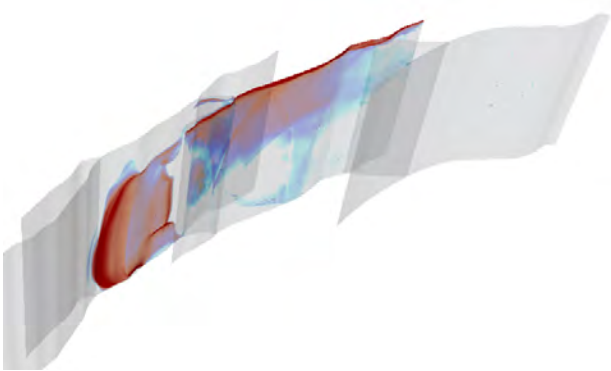
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Multiphysics Dynamic Rupture Simulation



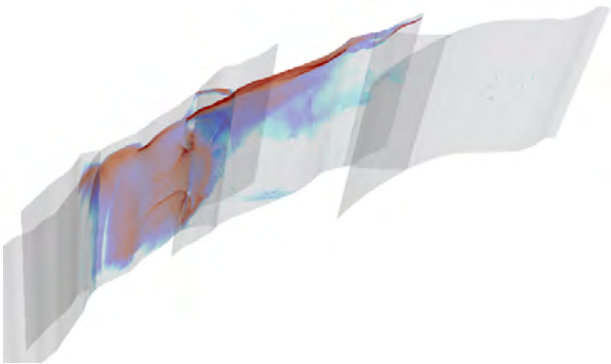
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Multiphysics Dynamic Rupture Simulation



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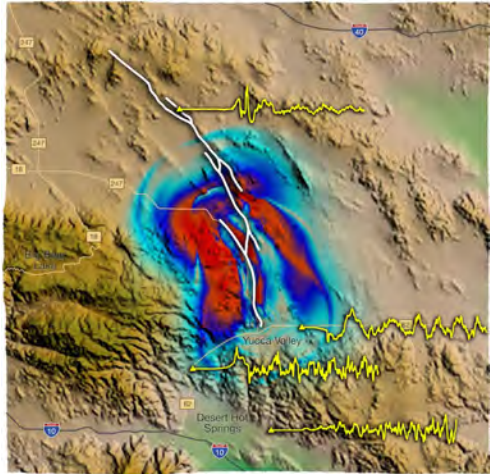
Landers Earthquake – Results

Observations:

- complex rupture dynamics (fault branching, etc.)
- high-frequency signals from rupture propagate directly into wave field
- synthetic seismograms with frequencies up to 10 Hz
- ground shaking in the engineering frequency band
- 42 s simulated time

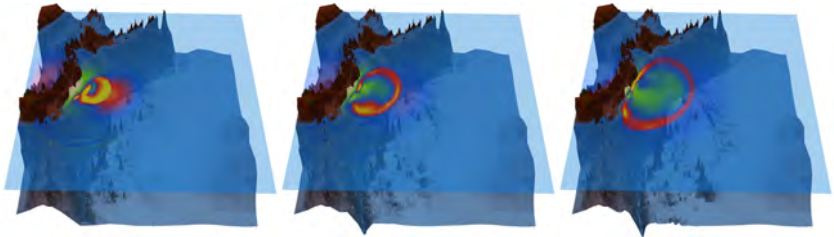
SuperMUC Production Run:

- **1.25 PFLOPS** sustained performance
- 7 h 15 min computing time



Project ASCETE

Simulation of Coupled Earthquake-Tsunami Events

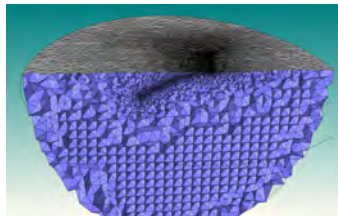


prototype simulation by P. Galvez [5] and K. Rahnema

Project Partners:

- earthquake simulation: C. Pelties, A. Gabriel, H. Igel (LMU Munich, **SeisSol**)
- seismology: L. Dalguer, P. Galvez (ETH Zürich)
- tsunami simulation: J. Behrens, S. Vater (Klima Campus, Univ. Hamburg)
- HPC: M. Bader, A. Breuer, K. Rahnema (TUM)

Simulation of Tsunamigenic Earthquakes



Tohoku subduction zone: CAD model and tetrahedral mesh (C. Pelties)

Challenges:

- curved subduction zones that meet surface at shallow angles
→ high impact on uplift for tsunamigenic earthquakes
- impact of time-dependent earthquake source on tsunami
→ near-field tsunami with long rupture process (Sumatra 2004)
→ near-field tsunami “double-slip” earthquake (Tohoku 2011)
- turning oceanic ground motion into shallow-water displacements

Part II

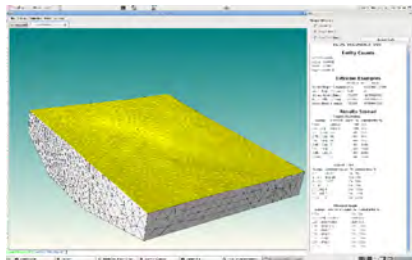
Scalable Meshing and I/O

Rettenberger, Smith, Pelties: *Parallel Unstructured Mesh Generation for the Petascale Application SeisSol*, poster, SC14.

Mesh Generation and Partitioning

Mesh Generation:

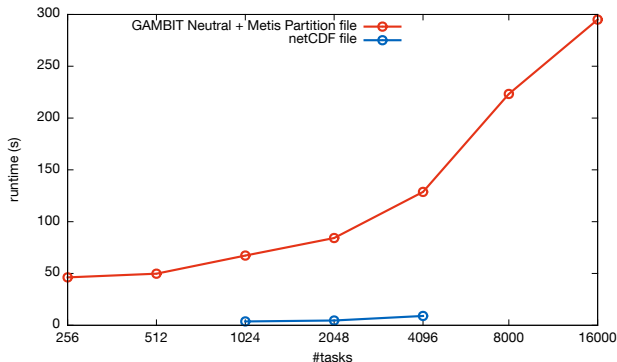
- high-quality meshes required (complicated fault structures, controllable mesh coarsening)
- with 10^8 – 10^9 grid cells
- using **SimModeler** by Simmetrix (<http://simmetrix.com/>)



Wanted: scalable solution to provide parallel mesh partitions

- graph-based partitioning (ParMETIS)
- create customised parallel format (based on netCDF) for mesh partitions (also contains information on neighbour partitions, etc.)
- highly scalable mesh input via netCDF/MPI-IO in SeisSol

Stating Point: Init Mesh Partitions in SeisSol



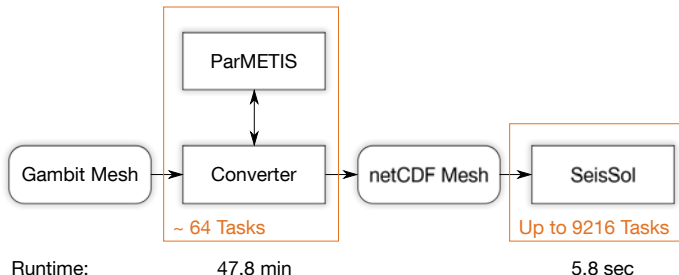
- strong scaling test on SuperMUC
- LOH.1 benchmark with 7,252,482 grid cells
- combine info from GAMBIT Neutral file and Metis Partition file
- does not scale, memory requirements per task: $O(\#cells)$

Two-stage Approach for Scalable Mesh Input

PUMgen: offline partitioning and mesh file generation

- start from mesh file as input
- call ParMETIS to compute partitions and communication structure
- write parallel mesh input file (based on netCDF format)

Resulting Mesh Pipeline:

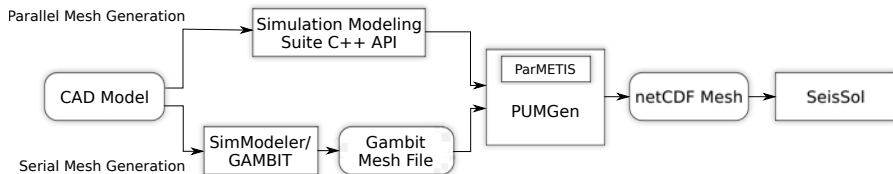


Two-stage Approach for Scalable Mesh Input (2)

PUMgen: offline parallel meshing and partitioning

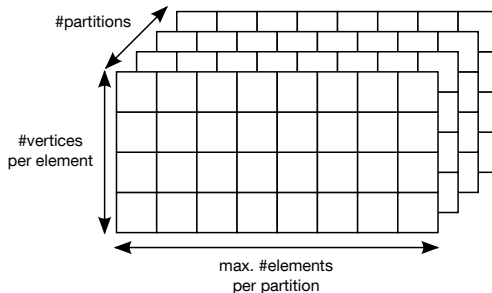
- start from CAD file as input
- parallel mesh generation via Simmetrix interface
- compute partitions and communication structure (ParMETIS)
- write parallel mesh input file (based on netCDF format)

Final Mesh Pipeline using PUMgen:

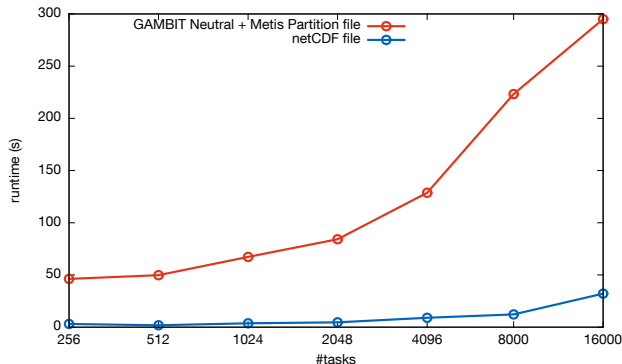


Parallel Mesh Input

- mesh and partition information combined in a single mesh file (binary file format: HDF5/netCDF)
- includes information on neighbour partitions
- includes information on partition boundaries (ghost layers, etc.)
- relies purely on collective MPI I/O operations to access data
- each processor only reads its own partition



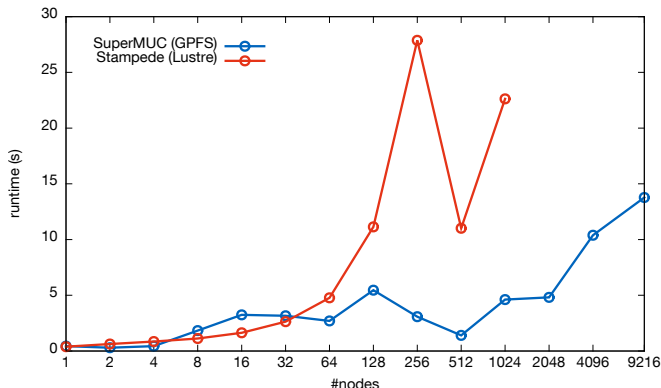
Parallel Mesh Format – Strong Scaling



- SuperMUC
- Strong scaling
- LOH.1
- 7,252,482 cells

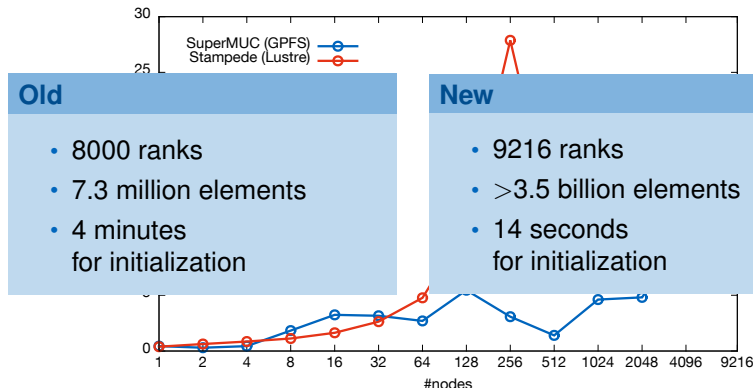
- Runtime and memory requirements are reduced to $O(\#cells/\#partitions)$
- largest test: mesh with 8,847,360,000 tetrahedrons read in 23 seconds on 9216 nodes/ranks

Parallel Mesh Format – Weak Scaling



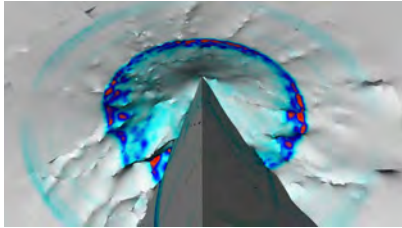
- Cubic domain, uniformly refined tetrahedral cells
- Weak scaling: 400,000 elements per node
- Largest mesh: > 3.5 billion cells

Parallel Mesh Format – Weak Scaling

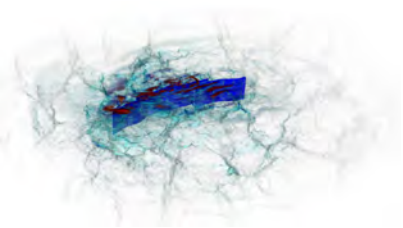


- Cubic domain, uniformly refined tetrahedral cells
- Weak scaling: 400,000 elements per node
- Largest mesh: > 3.5 billion cells

Wave Field Visualization for SeisSol



Volcano Mount Merapi

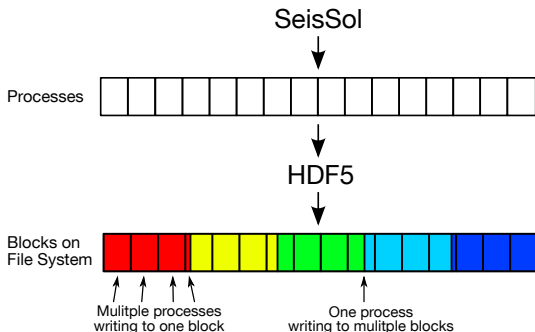


1992 Landers Earthquake

- only low-order data visualised
⇒ data sets are small (compared to computational cost)
- goal: aggregate all data into a single file
⇒ avoids creation of many small files & directory structures
- use **XDMF**: eXtensible Data Model and Format
(supported by Paraview and Visit, <http://xdmf.org/>)

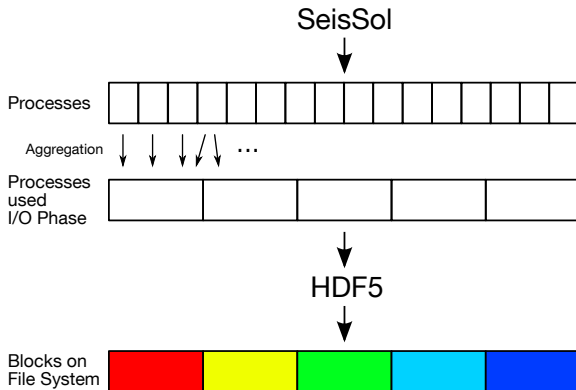
Writing to a Single File in Parallel

- Files can be partially locked by a process
- “Parts” are defined by the file system blocksize (GPFS)



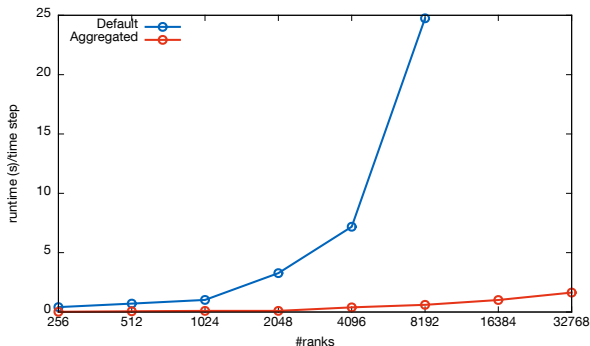
- SeisSol's chunks are small (~ 200 KB per process) compared to the blocksize (8 MB on SuperMUC)
- thus: acquiring locks becomes the bottleneck

Aggregate and Align Data



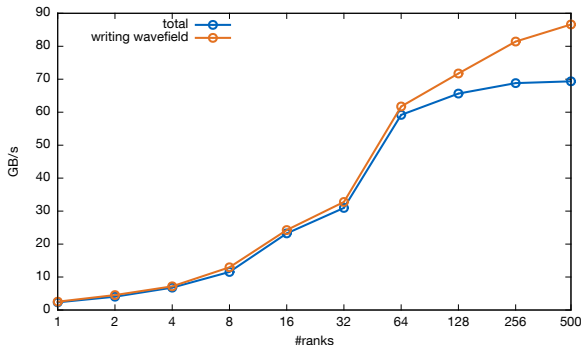
- Data is redistributed/aggregated to match file system blocks
- Not all processes may be included in the actual I/O phase

XDMF – First test application



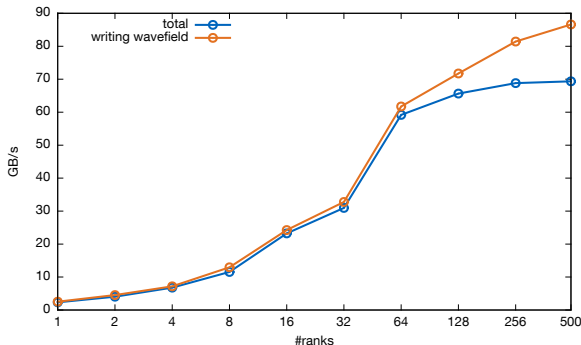
- $\sim 2 \times 78$ KB per process
(simulates $\sim 10,000$ elements with 2 variables per process)
- Exact element counts can vary ± 5 elements
(simulates load imbalance from partitioners)
- SuperMUC: GPFS with 8 MB blocksize

Checkpointing - Latest results



- Weak-scaling scenario with 640,000 elements per node, 6th order accuracy → Checkpoint size: 2.4 GB/node
- Total bandwidth includes additional overhead (writing metadata, flushing file, ...)

Checkpointing - Latest results



- GPFS on SuperMUC:
Theoretical peak bandwidth on 9,216 nodes: 200 GB/s
- Overhead for writing a checkpoint every 1,000 timesteps is less than 0.5%.

Part III

Optimizing Kernel Operations in SeisSol

Breuer et al. [1,2]
PRACE ISC Award 2014

Seismic Wave Propagation with SeisSol

Elastic Wave Equations: (velocity-stress formulation)

$$q_t + Aq_x + Bq_y + Cq_z = 0$$

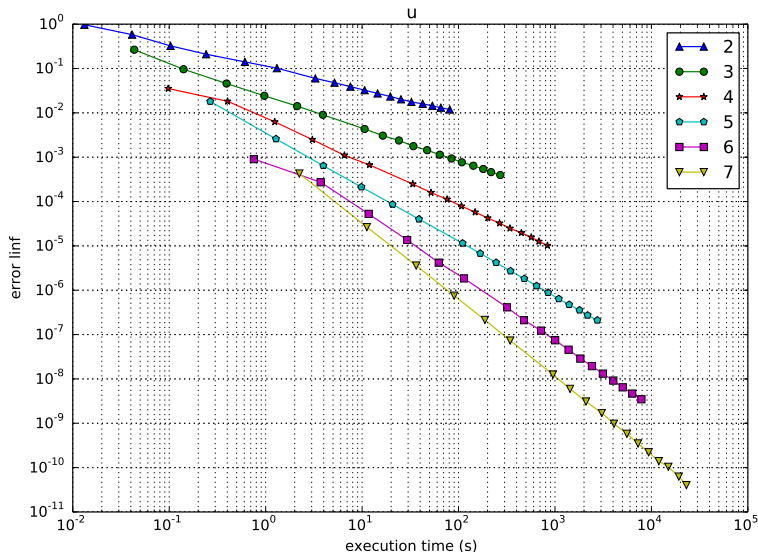
$$\text{with } q = (\sigma_{11}, \sigma_{22}, \sigma_{33}, \sigma_{12}, \sigma_{23}, \sigma_{13}, u, v, w)^T$$

$$A = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & -\lambda - 2\mu & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -\lambda & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -\lambda & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & -\mu & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -\mu \\ -\rho^{-1} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & -\rho^{-1} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & -\rho^{-1} & 0 & 0 & 0 \end{pmatrix} \quad B = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & -\lambda & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & -\lambda - 2\mu & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & -\lambda & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -\mu & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -\mu \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & -\rho^{-1} & 0 & 0 & 0 & 0 & 0 \\ 0 & -\rho^{-1} & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -\rho^{-1} & 0 & 0 & 0 & 0 \end{pmatrix}$$

- high order discontinuous Galerkin discretisation
- **ADER-DG**: high approximation order in space and time:
- additional features: local time stepping, high accuracy of earthquake faulting (full frictional sliding)

→ Dumbser, Käser et al. [4,6]

ADER-DG – Benefit of High Order



SeisSol in a Nutshell – ADER-DG

Update scheme

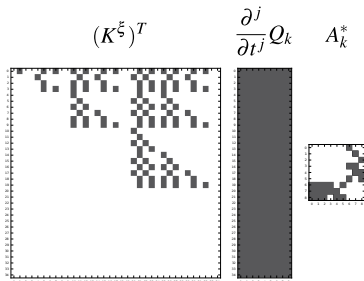
$$\begin{aligned}
 Q_k^{n+1} = Q_k - \frac{|S_k|}{|J_k|} M^{-1} & \left(\sum_{i=1}^4 F^{-,i} I(t^n, t^{n+1}, Q_k^n) N_{k,i} A_k^+ N_{k,i}^{-1} \right. \\
 & \left. + \sum_{i=1}^4 F^{+,i,j,h} I(t^n, t^{n+1}, Q_{k(i)}^n) N_{k,i} A_{k(i)}^- N_{k,i}^{-1} \right) \\
 & + M^{-1} K^\xi I(t^n, t^{n+1}, Q_k^n) A_k^* \\
 & + M^{-1} K^\eta I(t^n, t^{n+1}, Q_k^n) B_k^* \\
 & + M^{-1} K^\zeta I(t^n, t^{n+1}, Q_k^n) C_k^*
 \end{aligned}$$

Cauchy
Kovalewski

$$\begin{aligned}
 I(t^n, t^{n+1}, Q_k^n) &= \sum_{j=0}^J \frac{(t^{n+1} - t^n)^{j+1}}{(j+1)!} \frac{\partial^j}{\partial t^j} Q_k(t^n) \\
 (Q_k)_t &= -M^{-1} \left((K^\xi)^T Q_k A_k^* + (K^\eta)^T Q_k B_k^* + (K^\zeta)^T Q_k C_k^* \right)
 \end{aligned}$$

Optimisation of Matrix Operations

Apply sparse matrices to multiple DOF-vectors Q_k



Code Generator for Sparse Kernels: (Breuer et al. [1])

- avoid overhead of CSR (or similar) data structures; store CSR elements vector, only
- full “unrolling” of all element operations using a code generator
- use intrinsics and apply blocking to improve vectorisation

Code Generator – Sparse Matrix Kernels

```

stiffness_matrices_3d.hpp
stiffness_matrices_3d.hpp generatedMatrixMultiplication_kZetaT_3D_9_35(double* values, double* B, double* C)

7326 #endif
7327 #ifdef __SSE3__
7328     _mm128d b = _mm_loadup_pd(&B[(i*35)+11]);
7329     _mm128d c11_0 = _mm_loadu_pd(&C[(i*35)+0]);
7330     _mm128d a11_0 = _mm_loadu_pd(&values[32]);
7331     _mm_add_pd(c11_0, _mm_mul_pd(a11_0, b));
7332     _mm_storeu_pd(&C[(i*35)+0], c11_0);
7333     _mm128d c11_2 = _mm_loadu_pd(&C[(i*35)+2]);
7334     _mm128d a11_2 = _mm_loadu_pd(&values[34]);
7335     _mm_add_pd(c11_2, _mm_mul_pd(a11_2, b));
7336     _mm_storeu_pd(&C[(i*35)+2], c11_2);
7337     _mm128d c11_4 = _mm_loadu_pd(&C[(i*35)+4]);
7338     _mm128d a11_4 = _mm_loadu_pd(&values[36]);
7339     _mm_add_pd(c11_4, _mm_mul_pd(a11_4, b));
7340     _mm_storeu_pd(&C[(i*35)+4], c11_4);
7341     _mm128d c11_6 = _mm_loadu_pd(&C[(i*35)+6]);
7342     _mm128d a11_6 = _mm_loadu_pd(&values[38]);
7343     _mm_add_pd(c11_6, _mm_mul_pd(a11_6, b));
7344     _mm_storeu_pd(&C[(i*35)+6], c11_6);
7345     _mm128d c11_8 = _mm_loadu_pd(&C[(i*35)+8]);
7346     _mm128d a11_8 = _mm_loadu_pd(&values[40]);
7347     _mm_add_pd(c11_8, _mm_mul_pd(a11_8, b));
7348     _mm_storeu_pd(&C[(i*35)+8], c11_8);
7349 #else
7350     C[(i*35)+0] += values[32] * B[(i*35)+11];
7351     C[(i*35)+1] += values[33] * B[(i*35)+11];
7352     C[(i*35)+2] += values[34] * B[(i*35)+11];
7353     C[(i*35)+3] += values[35] * B[(i*35)+11];

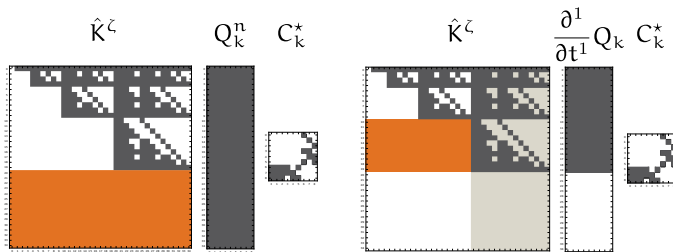
```

Code Generator – Dense Kernels



Optimisation of Matrix Operations

Apply sparse matrices to multiple DOF-vectors Q_k



Dense vs. Sparse Kernels: (Breuer et al. [2])

- switch to dense kernels depending on achieved time to solution
- for sparse and dense kernels:
exploit zero-blocks generated during recursive CK computation

Performance Optimization

Switch between Sparse/Dense Kernels:

- auto-tuning approach on benchmark scenarios
- measure sparse vs. dense performance for each matrix
- select sparse vs. dense kernel based on best time to solution

order							boundary
2	sparse	sparse	sparse	sparse	sparse	sparse	13%
3	sparse	sparse	dense	sparse	sparse	sparse	26%
4	sparse	sparse	dense	sparse	dense	dense	17%
5	sparse	sparse	sparse	sparse	sparse	sparse	23%
6	sparse	dense	dense	sparse	dense	dense	9%

Hybrid MPI+OpenMP Parallelisation:

- careful OpenMP parallelisation of all parts (not only main kernels → communication buffers, etc.)
- targeted at manycore platforms, such as Intel Xeon Phi
- OpenMP improvements for Xeon Phi also lead to noticeable improvements for “standard” CPUs

Part IV

Dynamic Rupture Simulation at Petascale – Xeon Phi Supercomputers

Heinecke et al.: *Petascale High Order Dynamic Rupture Earthquake
Simulations on Heterogeneous Supercomputers* [3]
ACM Gordon Bell Finalist 2014

Supercomputing Platforms

SuperMUC @ LRZ, Munich

- 9216 compute nodes (18 “thin node” islands)
147,456 Intel SNB-EP cores (2.7 GHz)
- Infiniband FDR10 interconnect (fat tree)
- #12 in Top 500: 2.897 PFlop/s



Stampede @ TACC, Austin

- 6400 compute nodes, **522,080 cores**
2 SNB-EP (8c) + **1 Xeon Phi SE10P** per node
- Mellanox FDR 56 interconnect (fat tree)
- #7 in Top 500: 5.168 PFlop/s



Tianhe-2 @ NSCC, Guangzhou

- 8000 compute nodes used, **1.6 Mio cores**
2 IVB-EP (12c) + **3 Xeon Phi 31S1P** per node
- TH2-Express custom interconnect
- #1 in Top 500: 33.862 PFlop/s



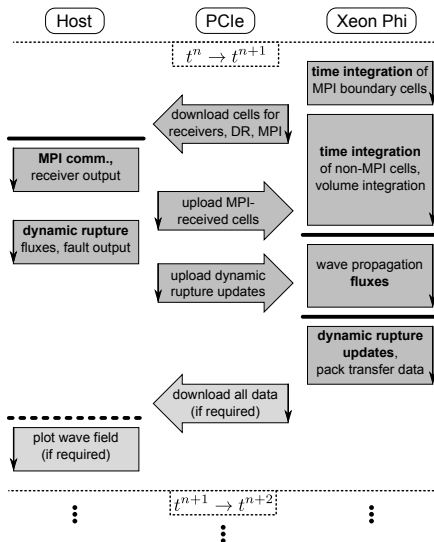
Optimization for Intel Xeon Phi Platforms

Offload Scheme:

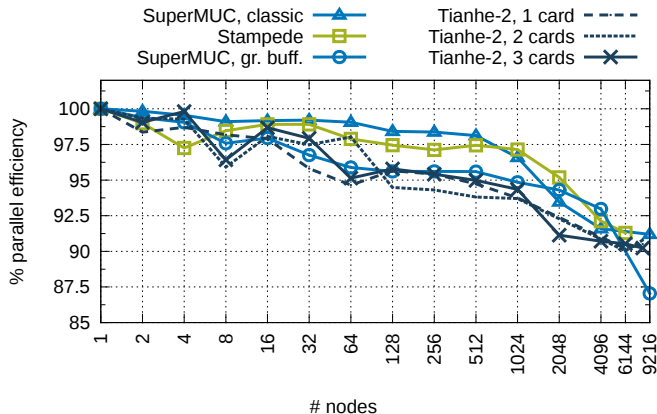
- hides communication with Xeon Phi and between nodes
- use “heavy” CPU cores for dynamic rupture

Hybrid parallelism:

- on 1–3 Xeon Phis and host CPU(s)
- reflects multiphysics simulation
- manycore parallelism on Xeon Phi

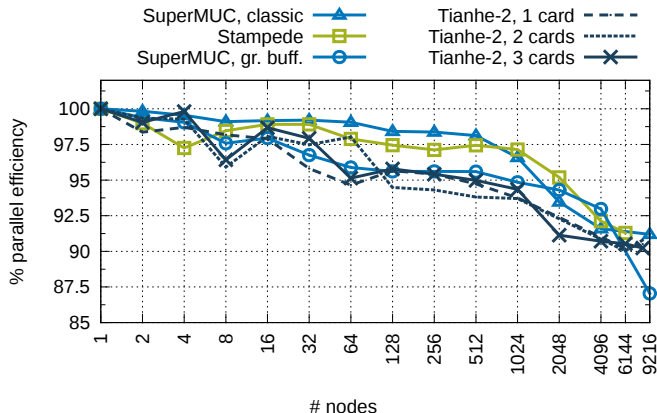


Weak Scaling of Wave Propagation



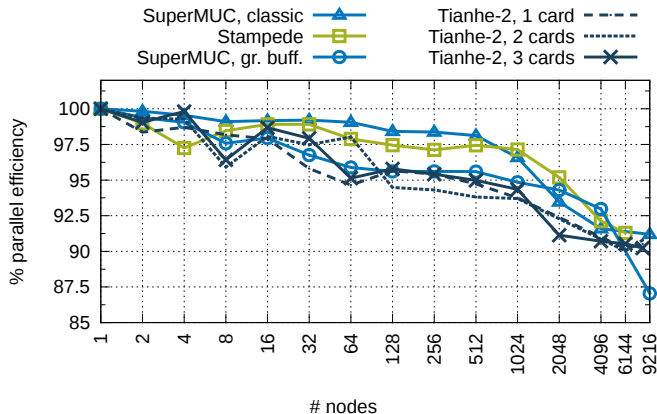
- goal: test scalability towards large problem sizes
- cubic domain, uniformly refined tetrahedral cells
- weak scaling: 400,000 elements per card/node

Weak Scaling of Wave Propagation



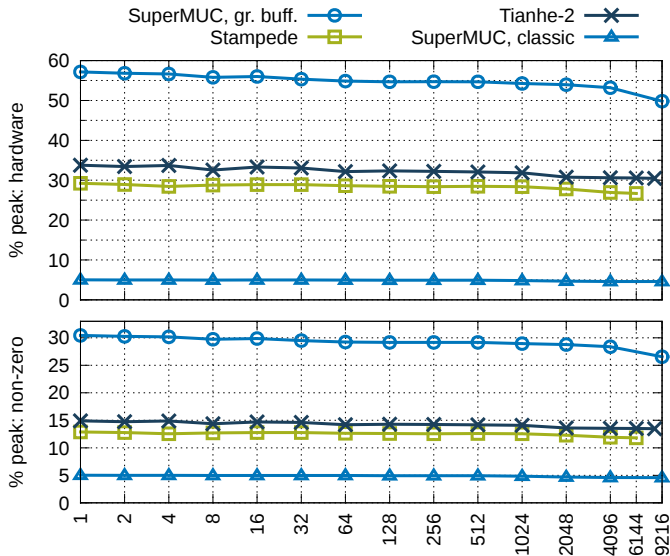
- more than 90 % parallel efficiency on Tianhe-2 and Stampede
- 87 % on full SuperMUC (no overlapping)

Weak Scaling of Wave Propagation

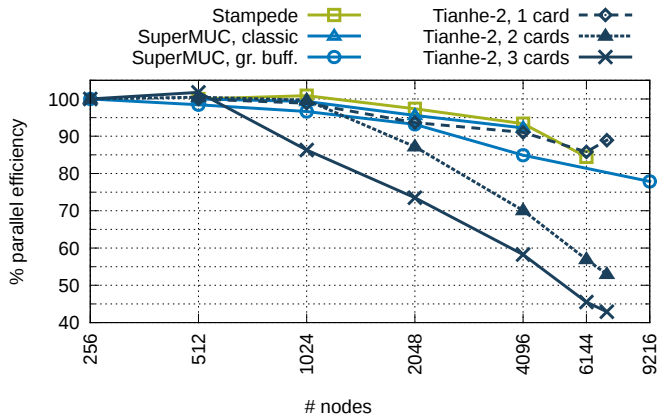


- 8.6 PFlop/s on Tianhe-2 (8000 nodes)
- 2.3 PFlop/s on Stampede (6144 nodes)
- 1.6 PFlop/s on SuperMUC (9216 nodes)

Weak Scaling – Peak Efficiency

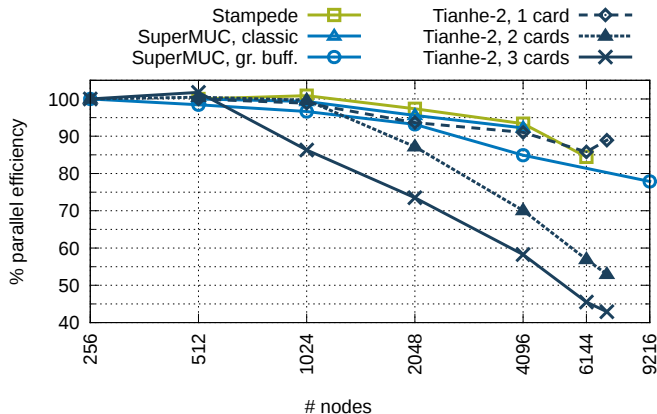


Strong Scaling of Landers Scenario



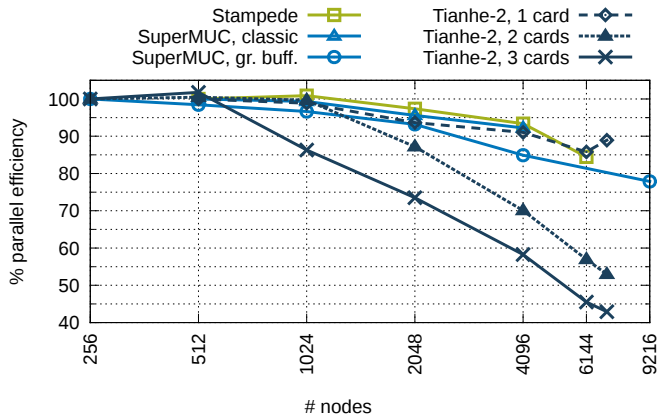
- 191 million tetrahedrons; 220,982 element faces on fault
- 6th order, 96 billion degrees of freedom

Strong Scaling of Landers Scenario



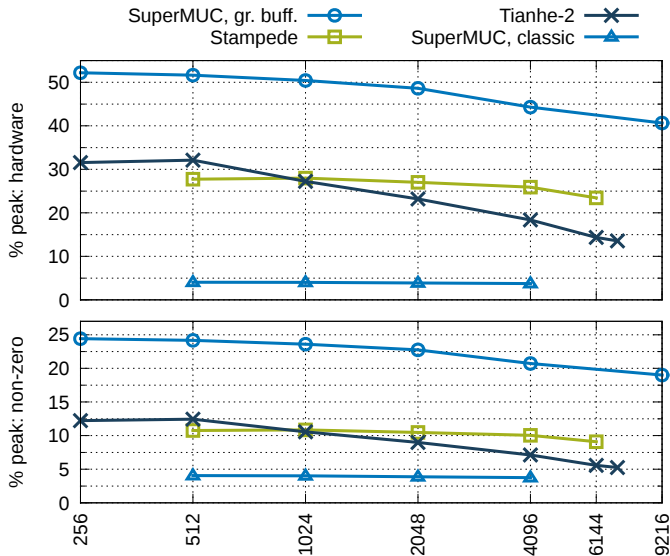
- more than 85 % parallel efficiency on Stampede and Tianhe-2 (when using only one Xeon Phi per node)
- multiple-Xeon-Phi performance suffers from MPI communication

Strong Scaling of Landers Scenario



- 3.3 PFlop/s on Tianhe-2 (7000 nodes)
- 2.0 PFlop/s on Stampede (6144 nodes)
- 1.3 PFlop/s on SuperMUC (9216 nodes)

Landers Strong Scaling – Peak Efficiency



SeisSol: Latest/Current Work on Optimization

Further Performance Engineering:

- improved memory layout: separate ghost/copy layers, NUMA awareness
- alignment of data for matrix kernels (esp. important for MIC)
- overlap computation and communication (using more effective data layout)
- improved matrix kernels: assembler/machine code, AVX2 for Haswell

Towards Local Time Stepping:

- communication of time-integrated variables (instead of simple ghost cell exchange)
- more asynchronous updates

SeisSol: Earthquake Simulation @ Petascale

Multiphysics Dynamic Rupture Simulations with SeisSol:

- high-order ADER-DG on complicated geometries
- non-linear interaction of rupture process and seismic waves
- physics-based seismic hazard analysis

Petascale Performance on Heterogeneous Platforms:

- scalable mesh input (and output) of more than 9 billion cells
- exploits high computational intensity of ADER-DG
- requires careful tuning of the entire simulation pipeline
- code generation to accelerate element kernels
- offload-scheme for multiphysics with Xeon Phi
- extreme (hybrid) parallelism with approx. 1.6 million cores

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 - German Research Foundation
 - KONWIHR
- the entire SeisSol team and all contributors

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