

# Information Flow and Program Analysis

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# Project Context

Work in progress from a joint project with G. Snelting (KIT)  
Information flow control for mobile components based on  
precise analysis of parallel programs

Part of priority programme 1496  
Reliably Secure Software Systems (RS3)  
funded by DFG (German Research Foundation)

Special thanks to Benedikt Nordhoff

# What This Talk is About

Theme:

How can program analysis-like technology help  
PDG-based information flow analysis?

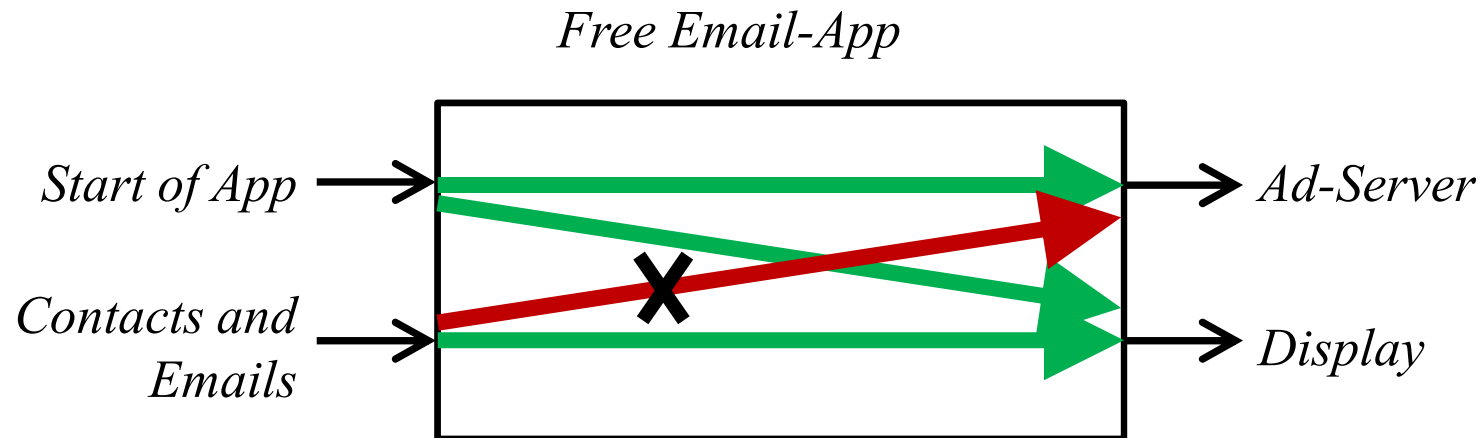
Program analysis:

Fixpoint-based methods:  
data-flow analysis, abstract interpretation

Information flow analysis:

see next slide

# Information Flow: Example



Reference scenario of SPP RS3:

- Software security for mobile devices
- Prototype of certifying app store for Android (Lortz et. al., ...)

# Non-Interference

For simplicity: transformational terminating programs only

Semantic setup:

Variables:  $\text{Var} = \text{Low} \cup \text{High}$   
States:  $\Sigma = \{ \sigma \mid \sigma : \text{Var} \rightarrow \text{Val} \}$   
Program semantics:  $\llbracket \pi \rrbracket : \Sigma \rightarrow \Sigma$

Low-equivalence of states:

$$\sigma \sim_L \sigma' \quad :\Leftrightarrow \quad \sigma|_{\text{Low}} = \sigma'|_{\text{Low}}$$

Program  $\pi$  is called non-interferent iff f.a.  $\sigma, \sigma' \in \Sigma$ :

$$\sigma \sim_L \sigma' \quad \Rightarrow \quad \llbracket \pi \rrbracket(\sigma) \sim_L \llbracket \pi \rrbracket(\sigma')$$

# Possibilistic Non-Interference

Semantics of non-deterministic programs:

$$\llbracket \pi \rrbracket : \Sigma \rightarrow 2^\Sigma$$

Refinement:

$$\pi \sqsubseteq \pi' \Leftrightarrow \forall \sigma: \llbracket \pi \rrbracket(\sigma) \subseteq \llbracket \pi' \rrbracket(\sigma)$$

Program  $\pi$  is called non-interferent iff f.a.  $\sigma_1, \sigma_2 \in \Sigma$ :

$$\sigma \sim_L \sigma' \Rightarrow \forall \rho \in \llbracket \pi \rrbracket(\sigma) : \exists \rho' \in \llbracket \pi \rrbracket(\sigma') : \rho \sim_L \rho'$$

**Observation:** Non-interference is not preserved by refinement.

Example:  $l := ?$  is non-interferent, its refinement  $l := h$  is not

Reason: Non-interference is a „hyper-property“

# A Fundamental Problem

- Abstraction is inherent to program analysis
- However, as just observed:  
    Non-interference does not transfer from abstractions
- Consequence:  
    Program analysis cannot be directly applied to non-interference

# Program Dependence Graphs (PDGs)

- A structure known from program slicing
- Nodes correspond to statements and conditions;  
we add artificial nodes for initial and final value of program variables
- Edges capture data dependences and control dependences
- PDGs can be applied for non-interference analysis

Analysis principle:

If there is no path in PDG from high input to low output  
then the program is non-interferent

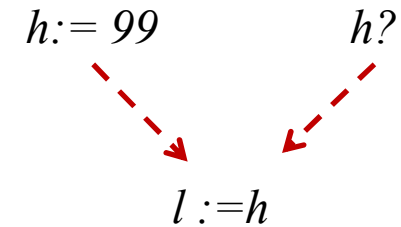


# Direct and Indirect Flows

Direct flows:

$l := h$

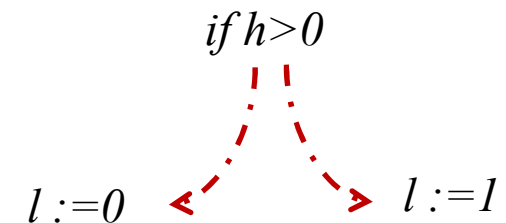
captured by **data dependence edges** in PDG



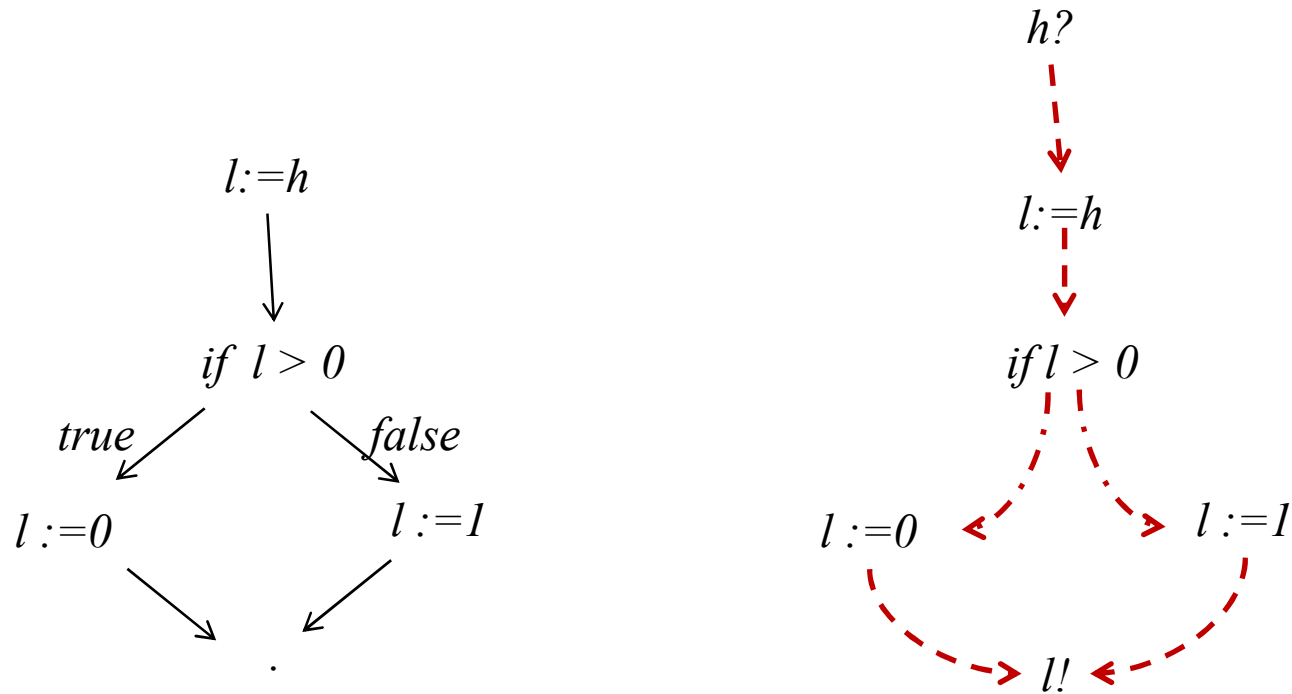
Indirect flows:

if  $h > 0$  then  $l := 0$  else  $l := 1$

captured by **control dependence edges** in PDG

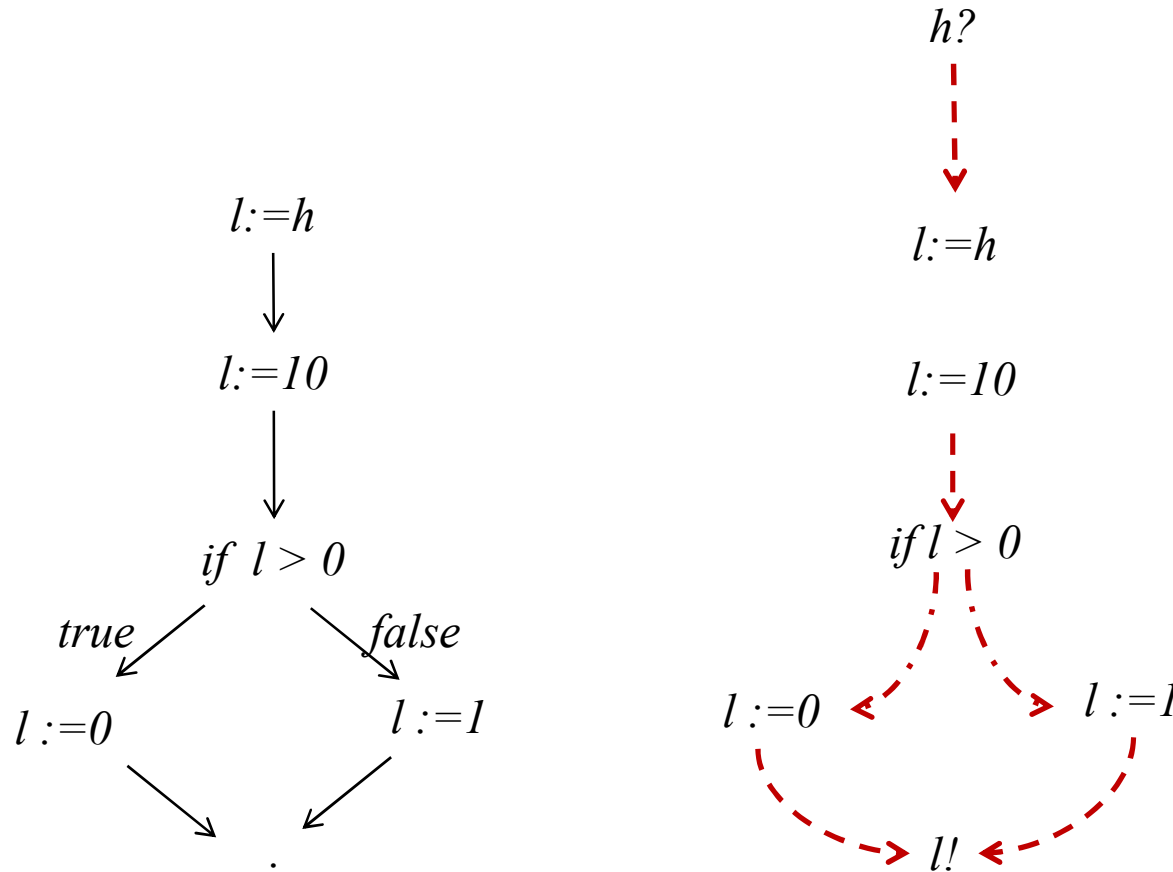


# Example 1



There is a path from  $h?$  to  $l!$ . Hence: Program may be interferent

## Example 2



There is no path from  $h?$  to  $l!$ . Hence: Program is non-interferent

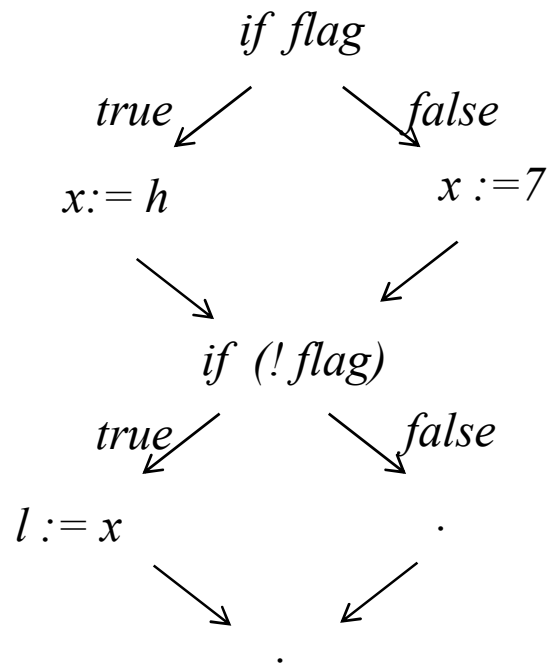
# Path Conditions

Goal: Improve precision of PDG-based dependence analysis

Idea: For each path in the PDG indicating critical flow, read off a necessary condition for flow from the guards. If all these conditions are unsatisfiable, there is no flow.

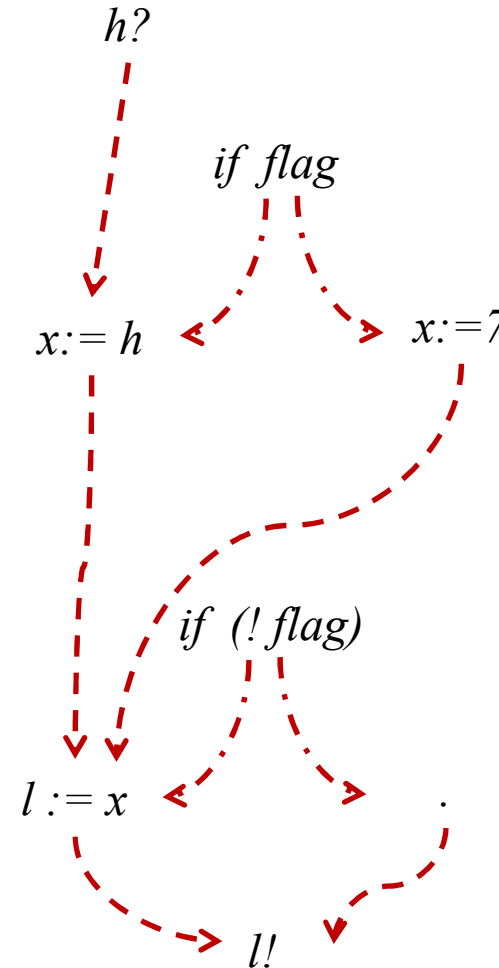
Caveat: Requires SSA-form of programs

# Path conditions improve precision of PDGs

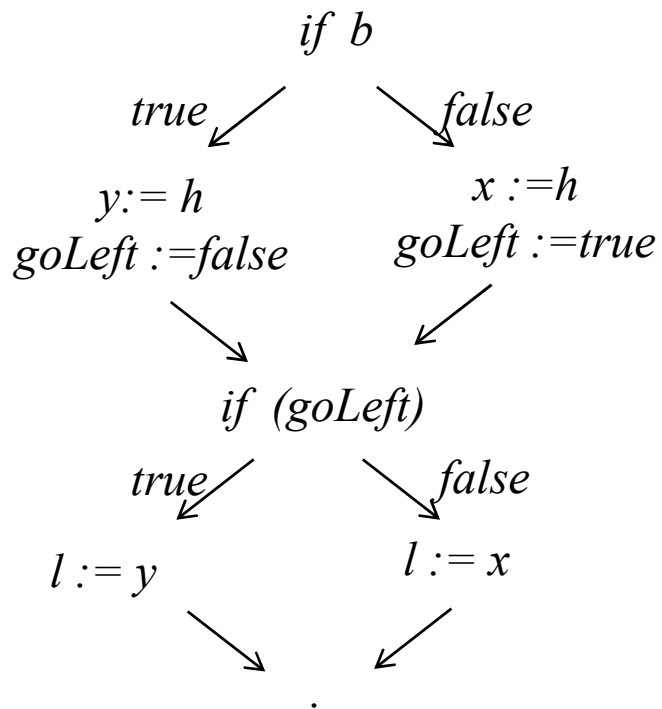


PDG alone: false alarm  
+ path conditions: OK

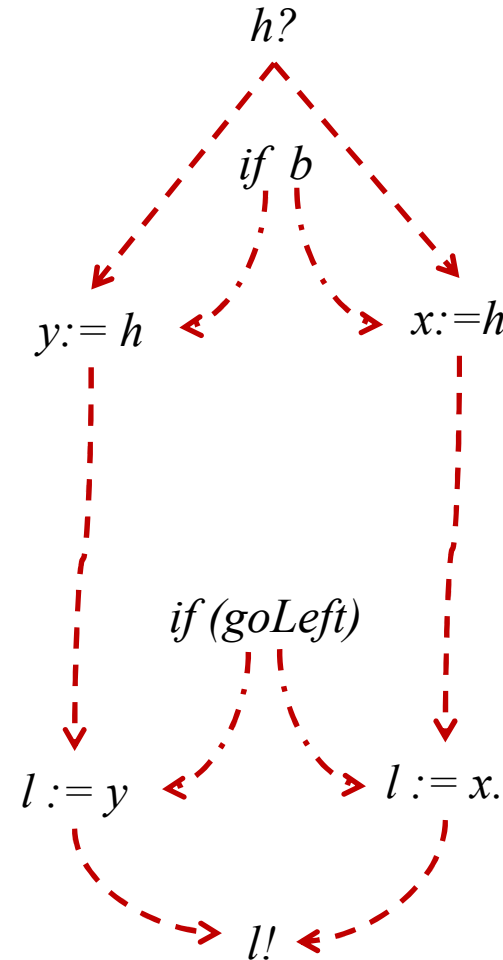
$flag \wedge ! flag$



# Further Improvements by Data Analysis Desirable



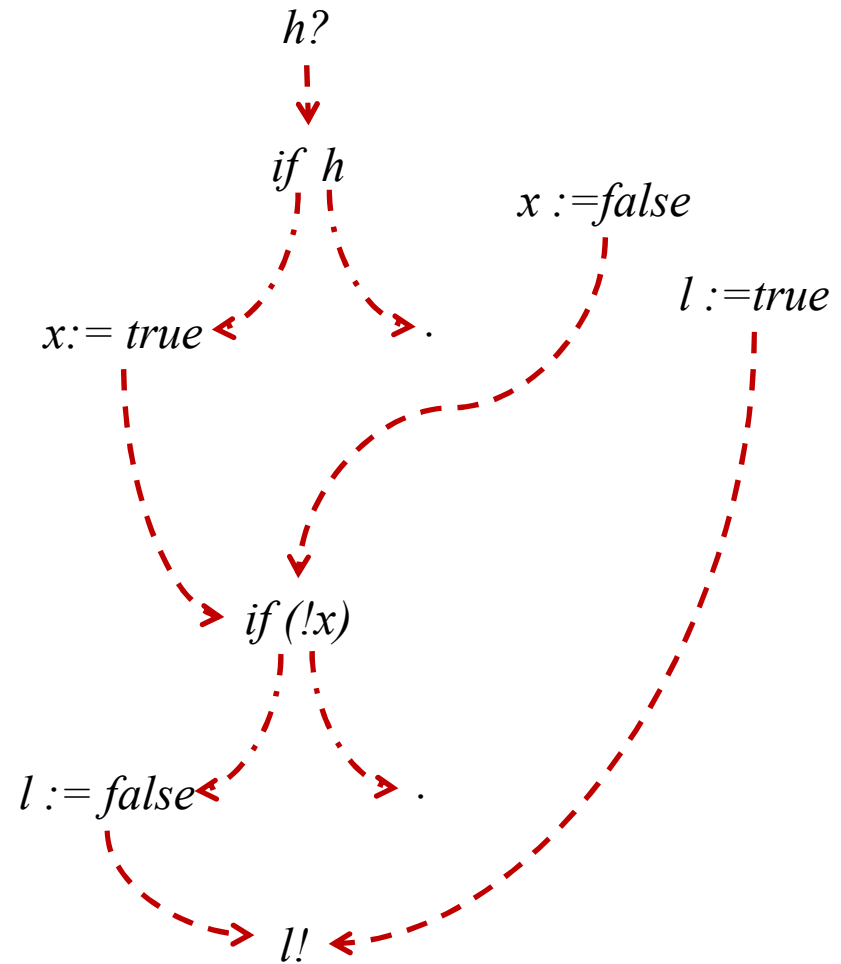
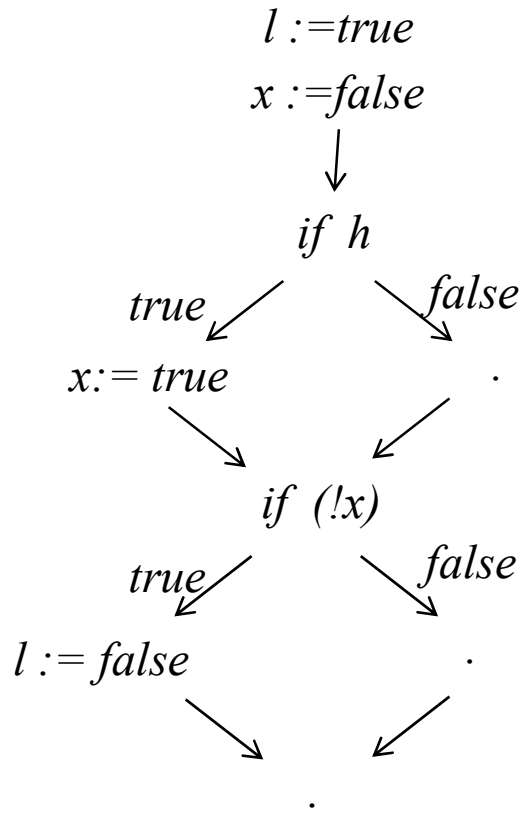
PDG + path conditions: false alarm  
+ invariant: OK



For left path:  $b \wedge goLeft \wedge goLeft = !b$

For right path:  $!b \wedge !goLeft \wedge goLeft = !b$

# The Show Stopper



PDG + path conditions  
+ invariant: unsound

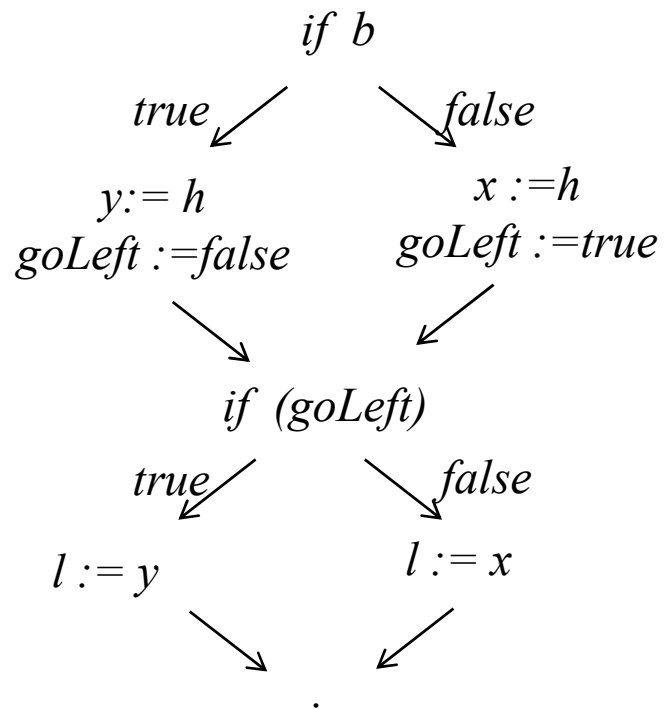
$$h \wedge !x \wedge x = h$$

# A Glimpse on Data Flow Slicing

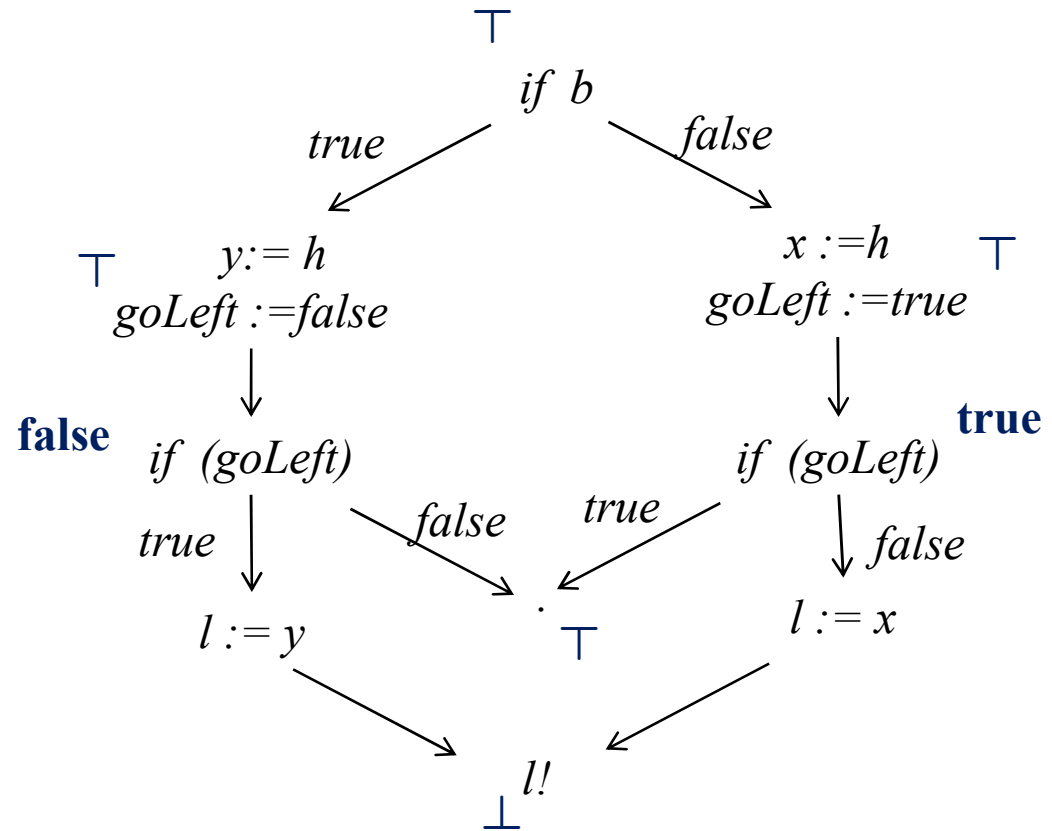
- Guiding intuition: Flow happens along PDG paths only
- Add new type of dependencies (data control dependencies) to avoid soundness problem
- Define executions along a PDG path
- Prove: If program has no execution along a critical PDG path, then program is non-interferent (Isabelle!)
- Actual analysis
  - Generate a program whose executions correspond exactly to the executions along critical PDG paths
  - Check by data flow analysis/abstract interpretation whether final control point is reachable
- Note: Approach allows to check non-interference by safety analysis !



# A Glimpse on Data Flow Slicing: Example



Original program



Generated program

Constant propagation on the generated program proves absence of critical information flow

# Discussion

Further work:

- Use DPNs to help PDG-based non-interference analysis of parallel programs based on LSOD
- Use DPNs to help type-based non-interference analysis of parallel programs

Alternative approaches:

- Self-composition
- Hyper-logics

Certifying App Store

# Thank you !